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KALMAN FILTER APPLICATION FOR FLEXIBLE SPACE SYSTEM PARAMETER IDENTIFICATION

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Abstract: Nowadays an increasing number of space missions are using satellites with a rigid hub and long and/or wide flexible appendices. such as solar panels, communication telescopic antennas, structures, robotics flexible arms. The increasing need for better pointing accuracy of antennas connected to the rigid part of the spacecraft leads to a requirement for more efficient controllers, where more accurate identification process play an important rule into the closed loop system. To meet the requirements for pointing accuracy, flexible parameters as elastic displacement, which are of great importance for control tasks should be continuously identified in the space environment. This paper presents an investigation results of elastic displacement identification using the Kalman Filter methodology. A flexible Euler-Bernoulli beam, connected to a rigid core with torques as input and angles and angular velocities as outputs is used as simple mathematical model of a rigid-flexible satellite to apply the Kalman filter identification algorithm proposed. The Kalman filter is tested under several conditions considering cold start with initial knowledge and varied coarse measurement noise levels. At the end comments are drawn about the robustness of the proposed procedure and feasibility of implementation within the control system loop.

1. Introduction

The use of small satellites has been a fast, simple and of low cost way of reaching the space in missions with the most several applications^{1, 2}, however, in order to conquer the space it is necessary to launch spacecraft that involves rigid/flexible structures. These missions are more complex because the satellites have a great number of components like, solar panels, antennas, cameras and mechanical manipulators. As a results, the influence of the flexibility of such structure play a important role in the dynamics behavior as well as in the performance of the Attitude Control System (ACS).³ Others important aspects in the study of the dynamics and control of flexible space structures are: the degree of interaction between the rigid and flexible motion, maintenance of the ACS performance in face the uncertainties of the mathematical model, damping residual vibrations in order to keep pointing precision and dynamic parameters identification.⁴ This paper presents an identification procedure using the Kalman Filter methodology that may be used to identify the elastic displacement and/or system parameters in space. Section 2 presents a mathematical model of a simple spacecraft based on a flexible Euler-Bernoulli beam connected to a rigid core. The equations of motion are also derived where the torque is used as input and angles and angular velocities as outputs. Section 3 presents the Kalman filter identification algorithm. Section 4 presents the simulation where the Kalman filter is tested under several conditions considering cold start with coarse initial knowledge and varied measurement noise levels. Section 5 concludes the paper.

2. Spacecraft Mathematical Model

The satellite mathematical model used is composed of a rigid platform with two flexible appendixes and masses in the extremities of the appendices. The appendices are identical and opposite, being considered as beam connected to the platform, and subjects to rotational and vibrational motion. In order to derive the equations of motion for this model, one applies the Lagrange methodology, starting from the expression of the kinetics and potential energy of the system. Fig. 1 illustrates the system composed by rigid hub, an elastic appendage with a mass in the extremity.



FIGURE 1. SATELLITE MODEL COMPOSED BY A RIGID HUB, AN ELASTIC APPENDAGE WITH A MASS IN THE EXTREMITY.

One considers that the inertial reference system, coincides with the origin of the fixed reference system in the rigid body and it is represented by the axes n_1 , n_2 , n_3 . The fixed reference system in the rigid body, coincides with the center of mass of the rigid body, which is characterized by the axes b_1 , b_2 , b_3 . The vector r represents the radius of the rigid body. The vector x represents a position of a measured mass element along the appendix in the no deformed form, in relation to the appendage reference system. The vector position of any point in the appendage relative to the inertial reference system is given by R. The vector of elastic displacement (elastic deformation) measured perpendicular to the axis b_1 is represented by y (x, t). Therefore, the vector position of any point in the deformed appendage form, relative to the inertial reference system is given for:

$$\underline{\mathbf{R}}_{1} = \left(\mathbf{r} + \mathbf{x}\right)\underline{\hat{\mathbf{b}}}_{1} + \mathbf{y}\underline{\hat{\mathbf{b}}}_{2} \tag{1}$$

and its velocity vector is

$$\underline{\mathbf{R}} = \frac{\mathrm{d}}{\mathrm{d}\,\mathrm{t}} \left(\underline{\mathbf{R}}\right)_{\mathrm{N}} = \frac{\mathrm{d}}{\mathrm{d}\,\mathrm{t}} \left(\underline{\mathbf{R}}\right)_{\mathrm{B}} + \underline{\boldsymbol{\omega}} \times \underline{\mathbf{R}} \qquad (2)$$

Considering that $\dot{\theta}$ is the satellite angular velocity and substituting Eq. (1) into (2), one has

$$\underline{\dot{R}} = -\dot{\theta} y \, \underline{\hat{b}}_1 + \left[\dot{\theta} \left(\mathbf{r} + \mathbf{x} \right) + \dot{y} \right] \underline{\hat{b}}_2 \qquad (3)$$

2.1. Equation of Motion

The total kinetics energy of the system is given by

$$\begin{split} \mathbf{T}_{\text{Total}} &= \mathbf{T}_{\text{disk}} + \mathbf{T}_{\text{app}} + \mathbf{T}_{\text{tip}} \\ \mathbf{T} &= \frac{1}{2} \mathbf{J}_{1} \dot{\boldsymbol{\theta}} + \dot{\boldsymbol{\theta}} \bigg[\int_{0}^{L} \rho(\mathbf{r} + \mathbf{x})^{2} \, d\mathbf{x} + \mathbf{m}_{t} \, (\mathbf{r} + \mathbf{x})^{2} + \mathbf{J}_{t} \bigg] + \\ &+ \int_{0}^{L} \rho \, \dot{\mathbf{y}}^{2} \, d\mathbf{x} + \mathbf{m}_{t} \, \left\{ \dot{\mathbf{y}}(\mathbf{L})^{2} \right\} + \mathbf{J}_{t} \, \left\{ \dot{\mathbf{y}}'(\mathbf{L}) \right\}^{2} + \\ &+ 2 \, \dot{\boldsymbol{\theta}} \left\{ \int_{0}^{L} \rho \, \dot{\mathbf{y}} \, (\mathbf{r} + \mathbf{x}) d\mathbf{x} + \mathbf{m}_{t} \, (\mathbf{r} + \mathbf{L}) \, \dot{\mathbf{y}}(\mathbf{L}) + \mathbf{J}_{t} \, \dot{\mathbf{y}}'(\mathbf{L}) \right\} \end{split}$$

$$(4)$$

where J_1 is the rigid body moment of inertia of the, ρ is the density of mass of the appendage, and L is the length of the appendage, m_t and J_t are the mass and moment of inertia of the mass at the end of the appendage and y(x, t) represents the elastic displacement.

The total potential energy V is considered as entirely due to the elastic deformations of the system and it is given by

$$V_{\rm T} = \frac{1}{2} \int_{0}^{L} (EI) \left(\frac{\partial^2 y}{\partial x^2}\right)^2 dx + \frac{1}{2} \int_{0}^{L} (EI) \left(\frac{\partial^2 y}{\partial x^2}\right)^2 dx = \int_{0}^{L} (EI) \left(\frac{\partial^2 y}{\partial x^2}\right)^2 dx$$
(5)

where E represents the module of elasticity (module of Young) and I the moment of inertia of the beam. The discretization of the system is done using assumed mode method.⁵ Therefore, the elastic displacement y(x,t) is substituted by

$$y(x,t) = \sum_{1}^{N} \phi_{j}(x) q_{ji}(t)$$
(6)

where $\phi_j(x)$ are the admitted functions and $q_{ji}(t)$ are the generalized coordinates. The equations of motion are found for the rotation $\theta(t)$ and elastic q(t) motion, using the Lagrange formulation

$$\frac{\mathrm{d}}{\mathrm{dt}} \left(\frac{\partial \mathrm{T}}{\partial \dot{\mathrm{x}}_{\mathrm{i}}} \right) - \frac{\partial \mathrm{T}}{\partial \mathrm{x}_{\mathrm{i}}} + \frac{\partial \mathrm{V}}{\partial \mathrm{x}_{\mathrm{i}}} = \mathrm{F}_{\mathrm{x}_{\mathrm{i}}} , \quad (i=1,2)$$
(7)

Substituting the kinetic and potential energy expression into Eq.(7) and after some manipulation the equations of motion are given by

$$J_{1}\ddot{\theta} + 2\ddot{\theta}\left[\int_{0}^{L}\rho(r+x)^{2}dx + m_{t}(r+L)^{2} + J_{t}\right] + 2\left[\int_{0}^{L}\rho(r+x)\phi_{i}(x)dx + m_{t}(r+L)\phi_{i}(x) + J_{t}\phi_{i}(L)\right]\ddot{q} = u$$
(8)

$$2 \ddot{\theta} \left\{ \int_{0}^{L} \rho(\mathbf{r} + \mathbf{x}) \phi_{i}(\mathbf{x}) d\mathbf{x} + m_{t}(\mathbf{r} + \mathbf{L}) \phi_{i}(\mathbf{L}) + \mathbf{J}_{t} \phi_{i}'(\mathbf{L}) \right\} + 2 \left\{ \int_{0}^{L} \rho \phi_{j}(\mathbf{x}) \phi_{i}(\mathbf{x}) d\mathbf{x} + m_{t} \phi_{j}(\mathbf{L}) \phi_{i}(\mathbf{L}) + \mathbf{J}_{t} \phi_{j}'(\mathbf{L}) \phi_{i}'(\mathbf{L}) \right\} \ddot{\mathbf{q}} + 2 \int_{0}^{L} (\mathbf{E}\mathbf{I}) \phi_{j}''(\mathbf{x}) \phi_{i}''(\mathbf{x}) q d\mathbf{x} = 0$$

(9)

The equations of motion in the matrix form is

$$\begin{bmatrix} \hat{\mathbf{J}} & \mathbf{M}_{\theta_{q}}^{\mathrm{T}} \\ \mathbf{M}_{\theta_{q}} & \mathbf{M}_{qq} \end{bmatrix} \begin{bmatrix} \ddot{\boldsymbol{\theta}} \\ \vdots \\ \ddot{\mathbf{q}} \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ 0 & \mathbf{K}_{qq} \end{bmatrix} \begin{bmatrix} \boldsymbol{\theta} \\ \mathbf{q} \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{u} \\ 0 \end{bmatrix}$$

$$(10)$$

where \hat{J} is the total inertia moment of the system, $M_{\theta q}$ represents the sub-matrix associated with the rigid and flexible motion, M_{qq} represents the sub-matrix associated with the flexible motion and K_{qq} represents the sub-matrix associated with flexible body. The matrix form in compact form is given by

$$\mathbf{M}\,\ddot{\mathbf{x}} + \mathbf{K}\,\mathbf{x} = \mathbf{D}\,\mathbf{u} \tag{11}$$

where M is the mass matrix, K is the stiffness matrix of the system and D is the control influence matrix.⁵ Eq.(12) in state space modal form is given by

$$\widetilde{\mathbf{M}} \ \ddot{\boldsymbol{\eta}} \ (t) + \widetilde{\mathbf{C}} \ \dot{\boldsymbol{\eta}} (t) + \widetilde{\mathbf{K}} \ \boldsymbol{\eta} (t) = \widetilde{\mathbf{D}} \ \mathbf{u} \tag{12}$$

where \widetilde{M} , \widetilde{C} , \widetilde{K} and \widetilde{D} represents mass, damping, stiffness and control influence matrices in modal form.

3. Kalman Filter Identification Algorithm

The Kalman filter is a computational algorithm containing a sequence of time and measurement updating of the estimates of the system state.⁶ The Kalman filter can incorporate dynamic noise in the dynamical model of the state. It is a real time estimator supplying the estimates for the instant that the measurement is available. The filter consists of two cycles:

- Time update
- Measurement update

In synthesis the Kalman filter processes measurements to produce an estimate of minimum variance of the state of a system using the knowledge of the dynamics of the system, and of the measurement, the statistics of the noise of the dynamic system, and errors of the measurements, besides the information of the initial condition.⁷

3. 1. State Dynamics Model

Let state dynamical model be represented by:

$$\dot{\mathbf{x}} = \mathbf{A}\mathbf{x} + \mathbf{G}\boldsymbol{\omega} \tag{13}$$

where $\mathbf{x} = (\theta, q, \dot{\theta}, \dot{q})$ is the state continuously variant in the time, G is a matrix of addition of dynamic noise, w is the continuous dynamic noise and A is named the system matrix that relates the state timely and linearly, given by:

$$\mathbf{A} = \begin{bmatrix} \mathbf{0} & | & \mathbf{I} \\ - - - - - - \\ - \tilde{\mathbf{K}} & | & -\tilde{\mathbf{C}} \end{bmatrix}$$
(14)

The system matrix is formed by the identity matrix I, by $\tilde{K} = \text{diag} \left\{ 0, \omega_2^2 \right\}$ the matrix containing the squared natural frequencies, and the modal damping matrix $\tilde{C} = \left\{ 0, 2\xi_2 \omega_2 \right\}$.

3. 2. Measurements Model

The measurement model is given by:

$$\mathbf{y} = \mathbf{H} \, \mathbf{x} + \mathbf{v} \tag{15}$$

where y is the measurement vector composed by the angle (θ) and angular velocity $(\dot{\theta})$ observable. The measurements θ and $\dot{\theta}$ are collected by a position and velocity sensor. For the angular position and velocity it was assumed nominally a standard deviation of 0.1° and 0.01° /s, respectively. The H matrix relates the measurements to the state by:

$$\mathbf{H} = \begin{bmatrix} 1 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 1 \ 0 \end{bmatrix} \tag{16}$$

and v represents a white noise vector to model the errors during the measurement process, with the following statistical characteristics

$$v_{\theta} = N(0, 0.1^{\circ}) \text{ and } v_{\theta} = (0, 0.01^{\circ} / \text{s})$$
 (17)

3. 3. Time update

In this filter cycle, the state and covariance estimates are computed by using the dynamical model of the system. The time updated state \overline{x} , and covariance \overline{P} are computed by:

$$\dot{\overline{\mathbf{X}}} = \mathbf{A}\,\overline{\mathbf{X}} \tag{18}$$

with initial condition $\overline{\mathbf{X}}_{k-1} = \hat{\mathbf{X}}_{k-1}$, and

$$\dot{\overline{P}} = A\overline{P} + \overline{P}A^{t} + GQG^{t}$$
⁽¹⁹⁾

with initial condition $\overline{P}_{k-1} = \hat{P}_{k-1}$. Equation (19) is known as the continuous Riccatti equation. In this work, Eq. (18) and (19) are solved numerically using the Runge-Kutta method embedded in the Matlab package.

3. 4. Measurement update

This cycle updates the state and covariance matrix at instant k due to measurement y_k , by means of the measurement model given by Equation (15). The measurements of instant k

provide the information to update the state and covariance. The equations that follow describe the measurement update cycle of Kalman filter:

$$\mathbf{K} = \overline{\mathbf{P}} \mathbf{H}^{\mathrm{t}} \left(\mathbf{H} \,\overline{\mathbf{P}} \,\mathbf{H}^{\mathrm{t}} + \mathbf{R} \right)^{-1} \tag{20}$$

$$\hat{\mathbf{P}} = \left(\mathbf{I} - \mathbf{K} \mathbf{H}\right) \overline{\mathbf{P}}$$
(21)

$$\hat{\mathbf{x}} = \overline{\mathbf{x}} + \mathbf{K} \left(\mathbf{y} - \mathbf{H} \,\overline{\mathbf{x}} \,\right) \tag{22}$$

where K represents the Kalman gain, and \hat{P} and \hat{x} are the covariance and the state updated. The errors between the actual state and the estimated state will be used to evaluate the algorithm performance for the tests carried out. The estimated error standard deviation were defined by:

$$\Delta \hat{\mathbf{\hat{e}}}_{i} = \mathbf{P}_{ii}^{\frac{1}{2}} \tag{23}$$

and the actual error

$$\Delta \varepsilon_{i} = x_{i} - \hat{x}_{i} \tag{24}$$

4. Simulations

The aim of the simulations is to implement and test the proposed Kalman filter methodology for identification of the flexible mode (elastic displacement) of a rigid flexible satellite. The analysis is performed through the utilization of the dynamical model equation (13) and Equations (15) to (22), which represent the time and measurement update of the state and covariance via the Kalman filter. The simulations were carried out by computational implementation of the software in Matlab language.

The investigation philosophy is, first of all, to analysis the nominal case using the initial conditions and parameters shown in Table 1. Next, the same conditions used in the nominal case are applied to analyze the behavior of the filter when non-typical measurement errors are imposed to the system. In particular, two cases comprising precise and imprecise measurements are shown and compared to the nominal case. It should be mentioned that in the space area the Kalman filter approach has been used for estimation of states associated with angular position and angular velocity and it is not of the autors' knowledge that this approach has been used before for flexible states estimation like displacements and its variation.

Symbol	Initial	Symbol	Initial	Symbol	Initial
	Values		Value		Value
G	I_4	$P_{\dot{\theta}}(^0\!/s)^2$	$(10)^2$	$Q_{\dot{\theta}}(^{0\!/\!s})^{2}$	10-6
$R_{\theta} \ (^{0})^{2}$	$(0.1)^2$	θ ₀ (°)	(0.1)	$\mathbf{P}_{\mathbf{\theta}}$ $(^{0})^{2}$	$(10)^2$
$R_{\dot{\theta}}(^0\!/\!s)^2$	$(0.01)^2$	$\dot{\theta}_0$ (%)	(0.01)	$Q_{\dot{q}}({}^{0\!/\!s})^{2}$	10-8
$Q_\theta \ ({}^0)^2$	10-6	Q_q (°) ²	10-8	$P_{q,q} \ (^0,/s)^2$	$(10)^2$

TABLE 1. INITIAL CONDITIONS AND TUNNED PARAMETERS OF THE KALMAN FILTER

4.1. Nominal Case

Figure 2 shows the actual and standard deviations for the angular position, elastic displacement, angular velocity, and rate of elastic displacement, in degrees and degrees/s respectively. Errors were calculated according to Eqs (23)-(24). From Figure 2, one notices that most of the actual errors are within one standard deviation of Eq. (23). Convergence was attained quickly (less than 20s) for all but the angular position, although it was within 0.05° from then on.



FIGURE 2. ANGULAR ERROR, ELASTIC DISPLACEMENT ERROR, ANGULAR VELOCITY ERROR, AND RATE OF ELASTIC DISPLACEMENT ERROR.

Figure 3 shows the behavior of the measurement residuals on θ and $\dot{\theta}$ for the nominal case. In this case the residuals are in good shape with one standard deviation around 0.1° and 0.01°/s, respectively.



FIGURE 3. RESIDUALS IN ANGULAR POSITION, AND RESIDUALS IN ANGULAR VELOCITY, NOMINAL CASE.

4. 2. Over-accurate measurements

In is case measurements are simulated with one order better accuracy. The aim is to verify if there is some relevant gain of accuracy in the identification filter when more accurate sensors are used. It can be observed in Figure 4 an apparent improvement in the residuals profile, one order better than the nominal case of Figure 3. This suggests better state estimates with respect to the nominal case. For this case the angular position and velocity measurements were corrupted with random gaussian noise of 0.01° e 0.001° /s, respectively.



FIGURE 4. RESIDUALS IN ANGULAR POSITION AND RESIDUALS IN ANGULAR VELOCITY, OVER ACCURATE MEASUREMENTS CASE

4.3. Under accurate measurements

In the same way, one investigated the effects of less accurate (than nominal) measurements, with the aim of verifying if the accuracy is degraded up to the extent the filter does not estimate the states correctly. From Figure 5 it can be seen the influence of increasing the measurement errors in the behavior of the estimation scheme. From the simulations it can be seen that even losing sensors accuracy the filter shape did not degrade when compared to the nominal case, in terms of convergence. The measurement errors in this case were random gaussian with 1° and 0.1°/s of standard deviation, respectively. The behavior of the residuals in this under accurate measurement case is shown in Figure 5. Consistently the residuals RMS also increased one order of magnitude with respect to the nominal case. Moreover, the states were estimates without sign of divergence of the Kalman filter.



FIGURE 5. RESIDUALS IN ANGULAR POSITION AND RESIDUALS IN ANGULAR VELOCITY, CASE OF UNDER ACCURATE MEASUREMENTS

Table 2 lists the mean and the standard deviation of the states corresponding to the rigid body and the flexible part of the satellite. Through the table it can be observed that for the three cases, namely nominal, over-accurate, and underaccurate measurements, the state components flexible regarding the body, (elastic q displacement) and \dot{q} , did not suffer any meaningful change in the mean and in the standard deviation error. Nevertheless, the state components of the rigid body, θ (angular position) and $\dot{\theta}$ (angular velocity), suffered as expected with the variation of the noise in the measurement. In relation to the nominal case, all the cases tested converged to the expected level of errors, showing the robustness of the filter under several levels of measurement accuracy.

	Nominal		
θ (⁰)	$(10^{-3}) \pm (2x10^{-1})$		
q (⁰)	$(3 \text{ x}10^{-2}) \pm (1.6 \text{ x}10^{-1})$		
$\dot{\boldsymbol{\theta}}$ (⁰ /s)	$(2.7 \text{ x} 10^{-4}) \pm (6 \text{ x} 10^{-2})$		
ḋ (⁰/s)	$(-1.23 \text{ x} 10^{-1}) \pm (4 \text{ x} 10^{-1})$		
	Over accurate		
θ (⁰)	$(-3.6 \times 10^{-4}) \pm (6 \times 10^{-2})$		
q (⁰)	$(3x10^{-2}) \pm (1.6x10^{-1})$		
$\dot{\boldsymbol{\theta}}$ (⁰ /s)	$(-5 \times 10^{-3}) \pm (6 \times 10^{-3})$		
ḋ (⁰/s)	$(-1.2 \text{ x} 10^{-1}) \pm (4 \text{ x} 10^{-1})$		
	Under accurate		
θ (⁰)	$(1.6 \times 10^{-2}) \pm (1 \times 10^{0})$		
q (⁰)	$(3x10^{-2}) \pm (1.6x10^{-1})$		
$\dot{\boldsymbol{\theta}}$ (⁰ /s)	$(7x10^{-2}) \pm (1.9x10^{-1})$		
ḋ (⁰/s)	$(-1.2 \times 10^{-1}) \pm (4 \times 10^{-1})$		

TABLE 2. MEAN AND STANDARD DEVIATION OF STATE ERRORS

5. Conclusion

In this work a satellite composed of a central rigid body and two flexible appendages was mathematically modeled to be used in an identification methology based on Kalman filter. A Lagrangian formulation was used to derive the equations of motion of the satellite. A discretization of the elastic motion was performed by the assumed mode method. In the sequel the Kalman filter methology using the Matlab package was implemented in order to identify the satellite rigid and flexible mode (states) composed of the rigid and elastic displacement and their variation in time. Throughout several simulations it was possible to investigate the behavior of the state estimation errors for three distinct cases. In the first one, called nominal case, typical data were considered as the initial conditions of the filter. In this case, it was verified that the satellite position and angular velocity error estimates are within the errors allowed by the filter, being observed a great time for the convergence of the filter in the angular position component. For the elastic displacement and rate the convergence has occur in less than 20 seconds.

Afterwards, two simulations considering nontypical conditions, that is, over accurate measurements and under accurate a measurement has been investigated. For the over accurate case (as expected) it was detected a remarkable improvement in the real and estimated states with respect to the nominal case, that fact is due to the more accurate sensors. In the under-accurate case, it was detected that even with less accuracy of the sensors, the estimated state errors were not so degraded with respect to the nominal case, keeping the filter convergence in acceptable level. Having in mind the complexity of putting a sensor on the elastic parts of the satellite, the application of the Kalman filter methology has been showed a good approach to identify indirectly the flexible parameters of a rigid-flexible satellite. That approach becomes more promising when it is necessary to feedback the elastic measurements into the control system in order to assure better pointing conditions and/or better system performance. The Kalman filter has also shown to be a robust methology since in the under-accurate case tested, it has maintained a good performance. Therefore, being an important tool in the parameters identification phase of similar control systems.

6. References

[1] Souza, L.C.G.; Silva, S. A., "Vibration Control of a Rigid-Flexible Satellite During Attitude Maneuver". Publicação da ASME do 17th Biennial Conference on Mechanical Vibration and Noise, 12-16, September, Las Vegas – Nevada, USA, 1999.

[2] Silva, A. R.; Schäfer, B.; Souza, L. C. G.; Fonseca, R. A., "Integrated Linear and Non-linear Parameters Identification for Space Robot Dynamics". *IAF - 51st International Astronautical Congress*. Out. 2000 - Rio de Janeiro, Brazil

[3] Silva, A.R.; Souza, L.C.G. "Control System Flexible Satellite Interaction During Orbit Transfer Maneuver". Published by American Astronautical Society (AAS) in Advances in the Astronautical Sciences, Vol. 100 Part I, pp. 541-550, paper AAS 98-343, Ed. Thomas H. Stengle, USA, 1998. ISBN 0-87703-453-2

[4] Silva, A R., Schäfer, B., Souza, L.C.G., "Identification and Sensor Failure Detection Algorithms Applied to Space Robotic Joint". XI Colóquio Brasileiro de Dinâmica Orbital, Viçosa-MG, Brazil, 04 a 08 de novembro de 2002.

[5] Trigolo, A e Souza, L.C.G.; "Attitude Control System Performance of Satellite". Presented CBDO – Congresso Brasileiro de Dinâmica Orbital, 20-24 de novembro, - Nazaré Paulista – SP, 2000 - Brasil.

[6] Gelb, A.; Kasper Jr., J.F.; Nash Jr., R.A.; Price, C.F; Sutherland Jr., A.A. Applied Optimal Estimation. Inglaterra: The M.I.T Press, 1974. 374p.

[7] Chiaradia, A. P. M., Determinação e Manobras Autônomas de Órbitas de Satélites Artificiais em Tempo Real usando Medidas GPS de uma Freqüência. São José dos Campos. Tese de Doutorado em Engenharia e Tecnologia Espacial-Instituto Nacional de Pesquisas Espaciais, 2002. INPE – 8755-TDI/198.